

9.3 D.C. MOTOR

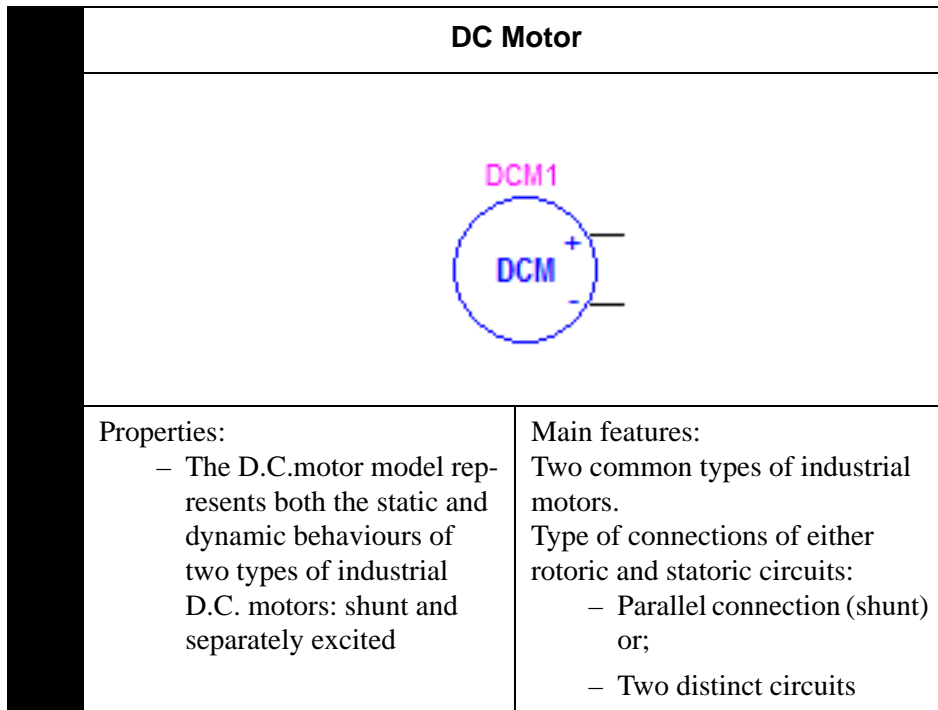


Figure 9 - 12 Icon and diagram DC motor

N –DC Motor Introduction

The following equations govern the voltages of the motor as a function of the currents:

$$v_f = r_f i_f + d\lambda_f/dt$$

$$v_a = r_a i_a + d\lambda_a/dt$$

where

- v_f : voltage at the terminals of the stator winding
- i_f : current in the stator
- r_f : resistance of stator winding
- λ_f : flux in the stator
- v_a : voltage at the terminals of the rotor winding
- i_a : current in the rotor
- r_a : resistance of the rotor winding
- λ_a : flux in the rotor

The fluxes can be expressed as follows:

$$\lambda_f = L_{ff}i_f + L_{fa}i_a$$

$$\lambda_a = L_{af}i_f + L_{aa}i_a$$

where

- L_{ff} : inductance in the stator winding
- L_{aa} : inductance in the rotor winding
- L_{af} et L_{fa} : mutual inductances between the rotor and the stator

Also, the mutual inductances can be estimated by a sinusoidal function of the angular speed of the motor Θ_c :

$$L_{af} = L_{fa} = -L\cos\Theta_c$$

where

- L is a constant

The action of the switch allows the rotor winding to be perceived as a stationary winding with a magnetic axis perpendicular to the axis of the winding field. There is no induced voltage in one of the windings because of the variation of the current crossing the other winding. Consequently, the voltage equations can be reduced to a matrix in a Laplace domain, as follows:

$$v_f(s) = r_f i_f(s) + sL_{ff}i_f(s)$$

$$v_a(s) = r_a i_a(s) + sL_{aa}i_a(s) + L_{af}i_f(s)$$

It is useful to represent the electromagnetic torque equation that follows:

$$T_e = L_{af}i_f i_a$$

And finally, using an equation linking the angular speed ω_r , a complete relation can be set and allows users to form the representative block diagram:

$$T_e = Jd\omega_r/dt + B_m\omega_r + T_L$$

where

- J : moment of inertia of rotor
- B_m : damping coefficient associated to the mechanical rotation movement
- T_L : load torque

Usually, the damping coefficient B_m is not considered.

The D.C. motor is often represented by Figure 9 - 13. According to the type of motor, the rotor circuit can be connected in parallel with the statoric circuit, thus $V_f=V_a$, in the case of a shunt motor.

A motor that uses two distinct circuits is referred to as a separately excited motor. The stator has to be supplied with another circuit, since the rotor is connected to the power network. The stator can be supplied using different methods, either using a constant source or with Simulink.

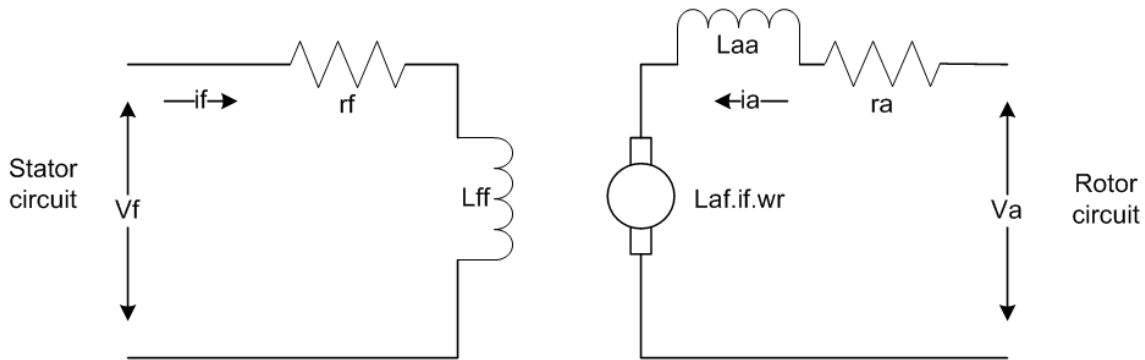


Figure 9 - 13 Simplified diagram of D.C. shunt motor

O –Motor Parameters

- R rotor: (r_a) resistance of rotor winding (ohm)
- L rotor: (L_{aa}) inductance of rotor winding (henry)
- R stator: (r_f) resistance of stator winding (ohm)
- L stator: (L_{ff}) inductance of stator winding (henry)
- L mutual: (L_{af}) mutual inductance between the stator and the rotor (henry)

P –Mechanical Load Parameters

- Load Torque: mechanical torque of the load driven by the motor (N.m)
- Moment of inertia: value of total inertia driven by the motor. This value consists of the inertia of the motor and the inertia of the driven mechanical load (kg.m^2)
- Viscous friction: value of viscous friction or damping. This corresponds to a friction loss varying with the speed (N.m.s)
- Dry friction: value of dry friction. This corresponds to constant friction loss (N.m)

Q – D.C. Motor Type

Allows users to specify the origin of the statoric circuit power supply:

- “Shunt connection”: the stator voltage is the same as the rotor voltage, since both are connected in parallel.
- “Internal”: separately excited motor, the stator is supplied by a constant internal source.
- “External”: separately excited motor, the stator is supplied by an external source originating from an A/D.
- “Simulink”: separately excited motor, the stator is supplied by a source originating from Simulink.

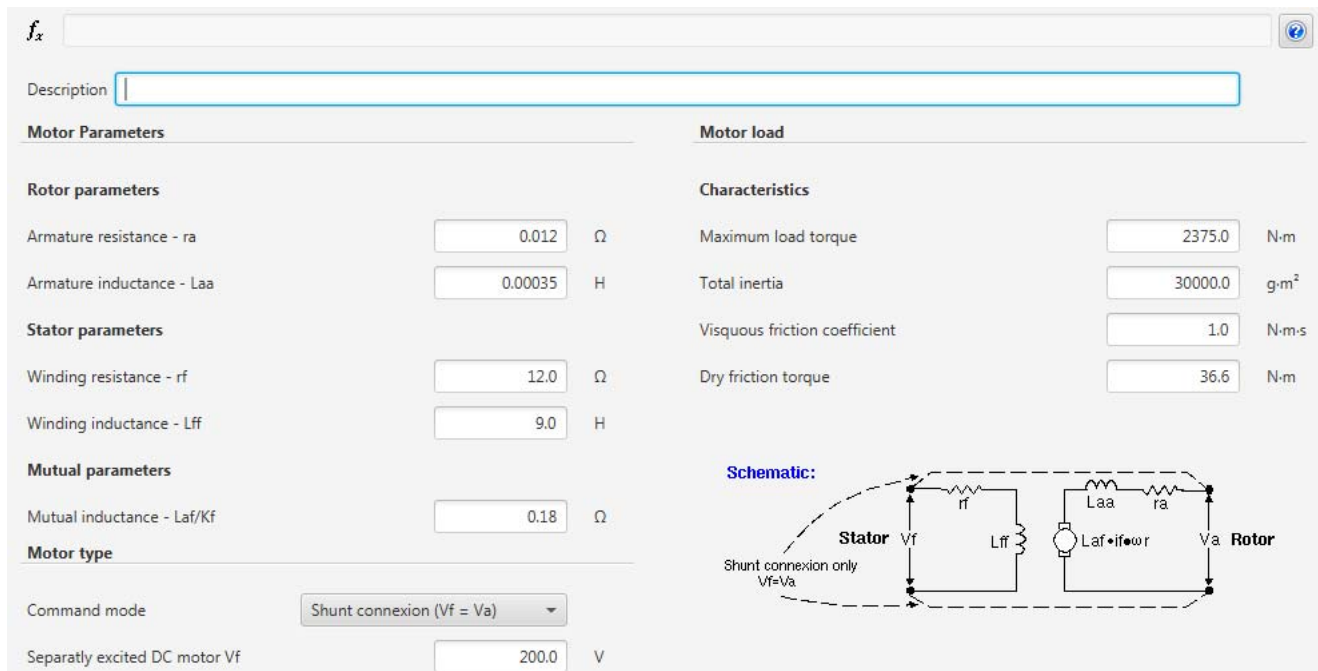
R – List of Available Signals

At acquisition, the following signals are made available by the sensors:

- I_{label} : total current of the D.C. motor (A)
- E_{label} : voltage generated by the armature circuit as a counter electromotive force (V)
- wr_{label} : speed of the D.C. motor rotor (rad/s)
- Vp_{label} : voltage at the positive terminal of the motor with respect to the ground (V)
- Vn_{label} : voltage at the negative terminal of the motor with respect to the ground (V)
- V_{ext_label} : voltage of the D.C. motor, or voltage of armature V_a (V)
- Vf_{label} : excitation voltage at the terminals of stator ($r_f + L_{ff}$) (V)
- $Vlink_label$: voltage originating from Simulink to supply the stator, in the case of a separately excited motor supplied by a Simulink circuit (V)
- Tm_{label} : mechanical torque of the motor load (N.m)
- If_{label} : current in the stator circuit or field current.

S – D.C. Motor Control Panel

Figure 9 - 14 shows the control panel of a D.C. motor.



f_x

Description

Motor Parameters		Motor load	
Rotor parameters		Characteristics	
Armature resistance - r_a	<input type="text" value="0.012"/> Ω	Maximum load torque	<input type="text" value="2375.0"/> N.m
Armature inductance - L_{aa}	<input type="text" value="0.00035"/> H	Total inertia	<input type="text" value="30000.0"/> g.m ²
Stator parameters		Visquous friction coefficient	<input type="text" value="1.0"/> N.m.s
Winding resistance - r_f	<input type="text" value="12.0"/> Ω	Dry friction torque	<input type="text" value="36.6"/> N.m
Winding inductance - L_{ff}	<input type="text" value="9.0"/> H		
Mutual parameters			
Mutual inductance - L_{af}/K_f	<input type="text" value="0.18"/> Ω		
Motor type			
Command mode	<input type="text" value="Shunt connexion (Vf = Va)"/>		
Separately excited DC motor V_f	<input type="text" value="200.0"/> V		

Schematic:

Shunt connexion only $V_f = V_a$

Stator: r_f , L_{ff}

Rotor: L_{aa} , r_a

Field winding: $L_{af} + i_f$

Terminal voltages: V_f , V_a

Figure 9 - 14 DC motor control panel



Figure 9 - 15 shows typical example using a DC Motor.

f_x ?

Description

Motor Parameters		Motor load	
Rotor parameters			
Armature resistance - ra	<input type="text" value="0.012"/>	Ω	
Armature inductance - Laa	<input type="text" value="0.00035"/>	H	
Stator parameters			
Winding resistance - rf	<input type="text" value="12.0"/>	Ω	
Winding inductance - Lff	<input type="text" value="9.0"/>	H	
Mutual parameters			
Mutual inductance - Laf/Kf	<input type="text" value="0.18"/>	Ω	
Motor type			
Command mode	Shunt connexion (Vf = Va)		
Separatly excited DC motor Vf	<input type="text" value="200.0"/>	V	

Characteristics

Maximum load torque	<input type="text" value="2375.0"/>	N-m
Total inertia	<input type="text" value="30000.0"/>	g-m ²
Visquous friction coefficient	<input type="text" value="1.0"/>	N-m-s
Dry friction torque	<input type="text" value="36.6"/>	N-m

Schematic:

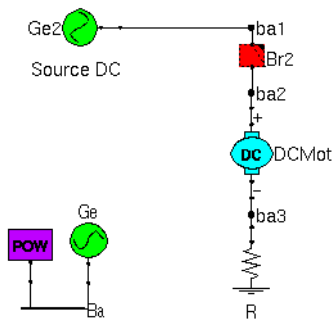


Figure 9 - 15 Example using a D.C. motor